CORRELATION BETWEEN RADICAL REACTIVITY AND QUANTUM CHEMICAL INDICES OF SUBSTITUTED PHENOIS

I. Iukovits, J. Kardos and M. Simonyi*<br>Central Research Institute for Chemistry of the Hungarian Academy of Sciences H-1025 Budapest, Pusztaszeri ut 59-67, Hungary. (Received in UK 30 May 1974; accepted for pablication 19 June 1974)

Polyvinyl acetate radicals abstract hydrogen atom from the $0 \rightarrow H$ group of phenols ${ }^{1}$

$$
\mathrm{R}^{\bullet}+\mathrm{Y}-\mathrm{OH} \xrightarrow{\mathrm{k}} \mathrm{R}-\mathrm{H}+\mathrm{Y}-\mathrm{O}^{\circ}
$$

The reactivities, $k$, relative to that of unsubstituted phenol, $k_{0}$, can be correlated with electrophilic substituent constants ${ }^{2 b}, 3$. For 18 phenol derivatives (Table 1) the equation is (Fig.1.a):

$$
\begin{equation*}
\log \mathrm{k} / \mathrm{k}_{0}=\underset{\left(-1,276 \sum 0,044\right)}{\infty} \sigma^{+}+0,228 \tag{1}
\end{equation*}
$$

significantly differing from the earlier Hammett equation ${ }^{2 b}$ ( $\mathcal{F}=-1,52$; Fig.1.b). The correlation coefficient, R, for Eq.(1) is 0,991. We have tried to find correlation between reactivities and quantum chemical indices too. The all-valence electron Extended Hückel method ${ }^{4}, 5$ has been applied for the computations. The computed atomic indices are : the net population, ${ }^{6} n$, the free valence, $F$, the frontier orbital density; ${ }^{8} f$, the charge density; $q$, the nucleophilic- and radical delocalizability, $S^{N}$ and $s^{R}$, the frontier orbital density in the first excited state and the squares of cuetficients of the lowest unoccupied molecular orbital. The computer program ${ }^{9}$ first selected the charge density, $q_{C_{1}}$, of the ring atom $C_{1}$. The regression equation is:

$$
\log k / k_{0}=\left(\begin{array}{c}
-14,339  \tag{2}\\
(1,693) \\
q_{1}
\end{array}+9,485\right.
$$

The correlation coefficient, $R$, for Eq. (2) is 0,904. Next variable to enter the regression equation was the total energy of the molecule divided by the number of valence electrons, $E_{n}$ :

$$
\begin{equation*}
10 g \mathrm{k} / k_{0}=\left(-13,638, q_{1},\left( \pm 0,233, E_{n}+4,627\right.\right. \tag{3}
\end{equation*}
$$

The correlation coefficient, $R$; for Eq. (3) is 0,756 . The measured and eatimated values of $\log k / k_{0}$ for 18 substituted phenols are summarized in Table 1.

Table 1
Measured and Estimated Reactivities of 18 substituted Phenols Towards Polyvinyl

## Acetate Radical

| No. | Molecule | Ref. | $\log k / k_{0}$ | Estimated Eq.(1) | values of Eq. (2) | $\begin{gathered} \log k / k_{0} \\ \operatorname{lq}_{0}(3) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Phenol | 2 a | 0,0 | 0,228 | 0,355 | 0,231 |
| 2 | 2-methylphenol | 2b | 0,447 | 0,625 | 1,080 | 0,851 |
| 3 | 2,6-dimethylphenol | 2b | 1,183 | 1,022 | 1,801 | 1,486 |
| 4 | 2,4,6-trimethylphenol | 2 a | 1,447 | 1,419 | 2,223 | 1,848 |
| 5 | 4-methylphenol | 2 b | 0,549 | 0,625 | 0,791 | 0,577 |
| 6 | 2,4-dimethylphenol | 2 b | 1,106 | 1,022 | 1,509 | 1,208 |
| 7 | 3-me thylphenol | $2 b$ | 0,449 | 0,312 | 0,298 | 0,108 |
| 8 | 3,5-dimethylphenol | 2 b | 0,315 | 0,397 | 0,239 | 0,001 |
| 9 | 2,3,5-trimethylphenol | 2b | 0,727 | 0,793 | 0,957 | 0,644 |
| 10 | Hydroquinone (HQ) | 2 b | 1,415 | 1,402 | 0,900 | 1,107 |
| 11 | HQ monoethyl ether | 2 b | 1,302 | 1,221 | 0,914 | 0,928 |
| 12 | p-hydroxybenzaldehyde | 2b | -0,477 | -0,387 | -0,796 | -0,576 |
| 13 | Pyrocatechol | 2 b | 1,660 | 1,402 | 1,267 | 1,455 |
| 14 | Resorcinol | 2b | 0,195 | 0,168 | 0,234 | 0,473 |
| 15 | Phloroglucinol | 2b | 0,125 | 0,108 | 0,098 | 0,634 |
| 16 | Pyrogallol | 2a | 2,682 | 2,576 | 2,222 | 2,652 |
| 17 | Durohydroquinone | 2 a | 2,444 | 2,364 | 2,173 | 1,999 |
| 18 | 5-hydroxypyrogallol | 11 | 3.478 | 3.750 | 2.780 | 3,422 |
|  |  |  | R: | 0,991 | 0,904 | 0,956 |

From these significant correlations ${ }^{10}$ the following conclusions can be drawne -the hydrogen atom donating ability of phenols decreases as the positive charge on atom $\mathrm{C}_{1}$ increases;

- it seems reasonable to assume correlation between the sum of electrophilic substituent constants and charge density on ring atom $C_{1}$;
- in spite of the high correlation coefficient of Eq. (1) the estimated value of $\log \mathrm{k} / \mathrm{k}_{0}$ for the molecule 5-hydroxypyrogallol exceeds significantly the experimental value ${ }^{12}$. The set of rate constants covers a broad range of 4 orders of magnitude and $\log k / k_{0}$ is a definitely curved function of electrophilic substituent constants (Fig.1.). The earlier Hamett equation ${ }^{2 b}$ covered a narrower range, hence the value of $\mathcal{G}$ differed from that of Eq.(1).

We emphasize that even the high correlation coefficients (e.g., 0,991 ) cannot guarantee the linearity of experimentally found correlations.

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Fig. 1. Correlation according to Eq.1.

